## MAT 296

For each of the following problems, indicate the correct partial fraction decomposition:

## Problem 1:

$$\frac{x-7}{x^2(x+3)}$$

(i) 
$$\frac{A}{x} + \frac{Bx + C}{x^2} + \frac{D}{x+3}$$
  
(ii) 
$$\frac{A}{x^2} + \frac{B}{x+3}$$
  
(iii) 
$$\frac{Ax + B}{x^2} + \frac{C}{x+3}$$
  
(iv) 
$$\frac{A}{x} + \frac{B}{x} + \frac{C}{x+3}$$

(v) None of the above

## Problem 2:

$$\frac{x^2 + x + 17}{x^2(3x+5)^2}$$

(i) 
$$\frac{A}{x^2} + \frac{B}{(3x+5)^2}$$
  
(ii)  $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{3x+5} + \frac{D}{(3x+5)^2}$   
(iii)  $\frac{A}{x} + \frac{Bx+C}{x^2} + \frac{D}{3x+5} + \frac{Ex+F}{(3x+5)^2}$   
(iv)  $\frac{A}{x} + \frac{Bx+C}{x^2} + \frac{Dx+E}{3x+5} + \frac{Fx+G}{(3x+5)^2}$ 

(v) None of the above

## Problem 3:

$$\frac{2x+13}{x^2(2x^2+5)^2}$$

(i) 
$$\frac{A}{x^2} + \frac{B}{2x^2 + 5} + \frac{C}{(2x^2 + 5)^2}$$
  
(ii)  $\frac{A}{x} + \frac{B}{x^2} + \frac{C}{2x^2 + 5} + \frac{D}{(2x^2 + 5)^2}$   
(iii)  $\frac{A}{x} + \frac{B}{x^2} + \frac{Cx + D}{2x^2 + 5} + \frac{Ex + F}{(2x^2 + 5)^2}$   
(iv)  $\frac{A}{x} + \frac{Bx + C}{x^2} + \frac{Dx + E}{2x^2 + 5} + \frac{Fx + G}{(2x^2 + 5)^2}$ 

(v) None of the above

**Problem 4:** A student is trying to solve  $\int \frac{x^6 - 2x^5 + 6x + 7}{x^2(x-5)} dx$ . As their first step, they break the fraction into

$$\frac{A}{x} + \frac{B}{x^2} + \frac{C}{x-5}$$

Is this a correct first step? If not, what should they have done first?

**Problem 5:** Integrate the following:

$$\int \frac{x+2}{x^2(x+1)} \, dx$$