Problem 1: Consider the following series. If the series converges, explain why and find the sum. If the series diverges, explain why.

$$\sum_{k=2}^{\infty} \frac{1}{3} \left(\frac{2}{e^2} \right)^k$$

Problem 2: Use the Comparison Test to prove the convergence or divergence of the following series:

$$\sum_{n=1}^{\infty} \frac{\cos^2 n}{n^4 + 2}$$

Problem 3: Determine whether the following series diverges or converges. [Hint: Divergence Test.]

$$\sum_{n=3}^{\infty} \frac{n^4 + n^2 - 7}{3n^4 - n^3 + 6}$$