

Problem 1: The plot of a function f(x) is given below. Use the plot to evaluate the following limits:

- (a) $\lim_{x \to 2^+} f(x) =$ (f) $\lim_{x \to -3} f(x) =$
- (b) $\lim_{x \to 2^{-}} f(x) =$ (c) $\lim_{x \to -3^{-}} f(x) =$ (d) $\lim_{x \to -3^{+}} f(x) =$ (e) $\lim_{x \to -\infty} f(x) =$ (f) $\lim_{x \to -\infty} f(x) =$
- (e) $\lim_{x \to 2} f(x) =$ (i) What are the roots of f(x)?

Problem 2: Evaluate the following limits. You do not need to justify your answer.

(a) $\lim_{x \to \infty} \frac{2x^2 - 5x + 7}{7x^3 - 2x^2 + 6} =$ (b) $\lim_{x \to \infty} \frac{2x^5 + 4x^2 + 7}{3x^5 - 4x^3 + 4x + 1} =$ (c) $\lim_{x \to \infty} \frac{2^x}{x^3 + 2x + 1} =$ (d) $\lim_{x \to \infty} \frac{5 \ln x}{x^2 + 2x + 3} =$ (e) $\lim_{x \to \infty} \frac{\sin x^2}{5^x} =$ (f) $\lim_{x \to \infty} \frac{x^2 + 7x + 3}{\sqrt{x - 3}} =$ (g) $\lim_{x \to \infty} \frac{\ln x}{\sqrt{x}} =$ (h) $\lim_{x \to \infty} \frac{x^3 + 5x + 9}{\sqrt{x^{10} - 4x + 6}} =$

Problem 3:

$$f(x) = \frac{(x+3)(x-2)(x+6)}{(x-2)(x+1)(x-3)}$$

- (a) What are the *x*-intercepts for f(x)?
- (b) What is the *y*-intercept for f(x)?
- (c) Where is f(x) continuous?
- (d) What are vertical asymptotes for f(x)?
- (e) What are the horizontal asymptotes for f(x)?
- (f) Does f(x) have any removable discontinuities? If so, what is the point?

Problem 4: Evaluate the following limit. Be sure to justify your answer completely: $\lim_{x \to -\infty} \frac{x^3 + 2x + 3}{x^2 + 6x + 1}$