

Name: \_\_\_\_\_

**Problem 1** (10 points) Let  $f(x, y) = 3xy + x^4 + y^3 + 1$ .

a) Compute the gradient vector of  $f$  at the point  $(1,2)$ .

b) Compute the directional derivative of  $f$  at the point  $(1,2)$  in the direction of  $\mathbf{u} = \langle 3/5, 4/5 \rangle$ .

**Problem 2** (10 points) Find the critical points of  $f(x, y) = 2x^2 - 4xy + y^4$ .