

***u*-substitution**

Integrate the following without using *u*-substitution. That is, any substitution must be done mentally only.

(a) $\int e^{x/2} dx$

(b) $\int \sin 5x dx$

(c) $\int \sec^2 2x dx$

(d) $\int 2^{3x} dx$

(e) $\int \frac{dx}{2x - 3}$

(f) $\int (x + 9)^3 dx$

More *u*-substitution

Integrate the following:

(a) $\int 2x\sqrt{x^2 + 3} dx$

(b) $\int \frac{3x}{\sqrt{2x^2 + 3}} dx$

(c) $\int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$

(d) $\int \frac{dx}{\sqrt{9 - x^2}}$

(e) $\int \frac{e^t}{9 + e^{2t}} dx$

(f) $\int \sqrt{1 - 4x^2} dx$ [Hint: Let $x = \frac{\sin \theta}{2}$]

Integration by Parts

Integrate the following:

(a) $\int x^3 \ln x \, dx$

(b) $\int x \sin x \cos x \, dx$

(c) $\int \frac{\ln x}{x^2} \, dx$

(d) $\int x^2 \sqrt{x-1} \, dx$

(e) $\int \arccos x \, dx$

Tabular Integration

Integrate the following by using Tabular Integration:

$$\int x^4 e^{x/2} \, dx$$

“Looping” Integrals

Integrate the following:

$$\int e^{5x} \cos 2x \, dx$$