

Name: \_\_\_\_\_  
Spring 2018

MAT 296: HW 6  
Due: 02/26

**Problem 1:** Determine whether the following improper integral converges or diverges. If it converges, give the value of the integral:

$$\int_0^\infty \frac{x}{(x^2 + 1)^2} dx$$

**Problem 2:** Determine whether the following improper integral converges or diverges. If it converges, give the value of the integral:

$$\int_2^6 \frac{dx}{6(x-2)^{3/2}}$$

**Problem 3:** Determine whether the following improper integral converges or diverges. If it converges, give the value of the integral:

$$\int_{-\infty}^{\infty} \frac{dx}{x^2 + 9}$$

**Problem 4:** Determine whether the following integral converges or diverges. If it converges, determine the value of the integral:

$$\int_{-\infty}^0 \sin \theta \, d\theta$$

**Problem 5:** Determine whether the following integral converges or diverges. If it converges, find its value.

$$\int_3^9 \frac{dx}{\sqrt{x^2 - 9}}$$

**Problem 6:** Determine whether the following integral converges or diverges. If it converges, find its value.

$$\int_{-2}^2 \frac{dx}{x}$$

**Problem 7:** Determine the values of  $p$  for which the integral

$$\int_e^\infty \frac{dx}{x(\ln x)^p}$$

converges. Find the value of the integral for these values of  $p$ .

**Problem 8:** Determine whether the following integral converges or diverges. [Hint: Try the Comparison Test for Integrals.]

$$\int_1^\infty \frac{\sin^2(e^x) + 3}{\sqrt[3]{8x^9 + 1729}} dx$$