

Name: _____
MAT 222
Fall 2019
Homework 1

*"I'm allergic to sushi. Every time I eat
more than 80 pieces, I throw up"*
–Andy Dwyer, *Parks and Recreation*

Problem 1: Watch ["Scientific Studies: Last Week Tonight with John Oliver \(HBO\)"](#). What did you learn from the video? Do you think the problems mentioned in the video are scientific problems or communication problems? Explain.

Problem 2: Watch [The Mathematics of History](#). What did you learn from the video? What implications does the proposals in the video have for Statistics and its role in society? What is question you would like to see investigated using Statistics (or Mathematics generally) in typically non-quantitative fields?

Problem 3: Each of the type of expressions below appeared in various statistical computations in MAT 221 and appear in MAT 222. Use a calculator to compute each of them.

(a) $\frac{1143.2 - 1434.8}{249.7} = \underline{\hspace{2cm}}$

(c) $\left(\frac{1.88 \cdot 8.7}{0.6}\right)^2 = \underline{\hspace{2cm}}$

(b) $\frac{31.5 - 27.6}{7.7/\sqrt{31}} = \underline{\hspace{2cm}}$

(d) $\frac{0.22 \cdot 0.81}{0.65 \cdot 0.91} = \underline{\hspace{2cm}}$

Problem 4: Each of the type of expressions below will appear in various statistical computations in MAT 222. Use a calculator to compute each of them.

(a) $\frac{9.2 - 8.3}{\sqrt{\frac{2.2^2}{24} + \frac{1.8^2}{22}}} = \underline{\hspace{2cm}}$

(c) $\frac{(31 - 1) \cdot 52.3^2 + (28 - 1) \cdot 53.4^2}{31 + 28 - 2} = \underline{\hspace{2cm}}$

(b) $\frac{87.3 - 81.4}{13.3 \cdot \sqrt{\frac{1}{15} + \frac{1}{18}}} = \underline{\hspace{2cm}}$

(d) $\sqrt{\frac{0.81(1 - 0.81)}{25} + \frac{0.86(1 - 0.86)}{22}} = \underline{\hspace{2cm}}$

Problem 5: There were 787 documented concussions from 1996–2001 in the National Football League (NFL).¹ Suppose the number of such head injuries followed the distribution $N(780, 121)$. Let X be the random variable representing the number of concussions in the NFL each year. Suppose also that *any* sample from the NFL always uses $N = 45$. Based on this information, complete the following chart:

| <u>x</u> | <u>z</u> | <u>Probability</u> |
|-----------------------|-----------------------|---|
| <u>902</u> | <u> </u> | <u>$P(X \leq x) =$</u> |
| <u>830</u> | <u> </u> | <u>$P(\bar{X} \leq x) =$</u> |
| <u>750</u> | <u> </u> | <u>$P(X \geq x) =$</u> |
| <u>750</u> | <u> </u> | <u>$P(\bar{X} \geq x) =$</u> |

¹<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3438866/>

Problem 6: You work for a technology firm that orders DDR4 memory chips in bulk. The company is opening up a new server data center and needs to order chips. Because no manufacturing process is perfect, some of the chips will be defective. The chip providers claim that no more than 1.5% of chips in any shipment are defective, on average. The company plans to order 1,200 chips from the company, though it only requires 1,170 to run the data center. What is the probability that the company will have too many defective chips to run the data center? Justify your work.

Problem 7: Suppose you have a sample with $x_1 = 1.7$, $x_2 = 2.0$, $x_3 = 3.1$, and $x_4 = -2.3$. Find the sample standard deviation, s , and also find $\sum_{i=1}^4 (x_i - \bar{x})^2$.