Name:
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MAT 222
Spring 2019
Chapter 9 Worksheet
"Maybe life is like a cross country road trip. You can get so focused on the enormity of the mission ahead, staring straight out of the expansive road as you fail to notice the stuff you're passing by right at that moment."

- Ginger Foutley, As Told By Ginger

Problem 1: A group of researchers is trying to determine if there is a relationship between ones education level and whether one has found employment. They survey a group of individuals, asking whether they are employed full-time, part-time, or are unemployed. They also ask the individuals whether they have a high school education, some college education (Associates), a B.A., a masters, or a Ph.D.. The results are summarized in the first table below. Complete the missing entries in the tables below.

Table of Counts

|  | High School | Associates | B.A. | Masters | Ph.D. | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Full-Time | 33 | 48 | 59 | 55 | 59 | 254 |
| Part-Time | 22 | 37 | 36 | 37 | 28 | 160 |
| Unemployed | 15 | 26 | 12 | 13 | 9 | 75 |
| Total | 70 | 111 | 107 | 105 | 96 | 489 |

Table of Expected Values

|  | High School | Associates | B.A. | Masters | Ph.D. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Full-Time | 36.36 | 57.66 | 55.58 | 54.54 | 49.87 |
| Part-Time | 22.90 | 36.32 | 35.01 | 34.36 | 31.41 |
| Unemployed | 10.74 | 17.02 | 16.41 | 16.10 | 14.72 |

Table of Chi-Squared Contributions

|  | High School | Associates | B.A. | Masters | Ph.D. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Full-Time | 0.3105 | 1.6173 | 0.2106 | 0.0039 | 1.6735 |
| Part-Time | 0.0354 | 0.0128 | 0.0280 | 0.2035 | 0.3704 |
| Unemployed | 1.6933 | 4.7380 | 1.1856 | 0.5984 | 2.2252 |

Perform a chi-squared analysis to determine if there is a relationship between ones employment and education level. Be sure to state your $H_{0}, H_{a}$ in the context of the problem, the degrees of freedom, your $p$-value, and your conclusion in the context of the problem. [Use $\alpha=0.10$.]

## Solution.

$X^{2}=$ sum of the entries of the last table $=14.9064$ degrees of freedom $=(5-1)(3-1)=8$
$\left\{\begin{array}{l}H_{0}: \text { there is no assoc. between Ed. \& Employ. } \\ H_{a}: \text { there is an assoc. between Ed. \& Employ. }\end{array}\right.$
Then we have $0.05<p<0.10$. Therefore, we reject the null hypothesis. There is an association between ones education level and their employment status.

Problem 2: Cornaught University is investigating whether they are admitting under-represented groups 'fairly' or if income may have some influence in admittance. They collect family income data on all African-American students at the University. The breakdown of the students' income levels is given in the table below. Given that $22 \%$ of African-Americans make under $15 \mathrm{~K}, 27 \%$ make between 15 K and $35 \mathrm{~K}, 38 \%$ make between 35 K and $100 \mathrm{~K}, 11 \%$ make between 100 K and 200 K , and $2 \%$ make over 200 K , determine whether the students are being admitted 'fairly'. [Use $\alpha=0.01$.]

| Income Level | $<15 \mathrm{~K}$ | $15 \mathrm{~K}-35 \mathrm{~K}$ | $35 \mathrm{~K}-100 \mathrm{~K}$ | $100 \mathrm{~K}-200 \mathrm{~K}$ | $>200 \mathrm{~K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Number of Students | 213 | 312 | 425 | 200 | 100 |

Solution. A total of 1,250 students were examined. This gives us an expected table of...

| Income Level | $<15 \mathrm{~K}$ | $15 \mathrm{~K}-35 \mathrm{~K}$ | $35 \mathrm{~K}-100 \mathrm{~K}$ | $100 \mathrm{~K}-200 \mathrm{~K}$ | $>200 \mathrm{~K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Expected Number of Students | 275 | 337.5 | 475 | 137.5 | 25 |

For example, the expected value in the second column is computed via $1250 \cdot 0.27=337.5$. This gives a contribution to $\chi^{2}$-table of...

| Income Level | $<15 \mathrm{~K}$ | $15 \mathrm{~K}-35 \mathrm{~K}$ | $35 \mathrm{~K}-100 \mathrm{~K}$ | $100 \mathrm{~K}-200 \mathrm{~K}$ | $>200 \mathrm{~K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\chi^{2}$-Contribution | 13.98 | 1.93 | 5.26 | 28.41 | 225.00 |

We have null and alternative hypotheses:

$$
\left\{\begin{array}{l}
H_{0}: \text { The data is consistent with the given percentages. } \\
H_{a}: \text { The data is not consistent with the given percentages. }
\end{array}\right.
$$

We have test statistic $X^{2}=13.98+1.93+5.26+28.41+225=275.58$ with degrees of freedom $5-1=4$. This gives $p$ value of $p \approx 0.000$. Therefore, we reject the null hypothesis. The rate of admittance of African-American students is not consistent with the known percentages of wealth rates of African-Americans.

